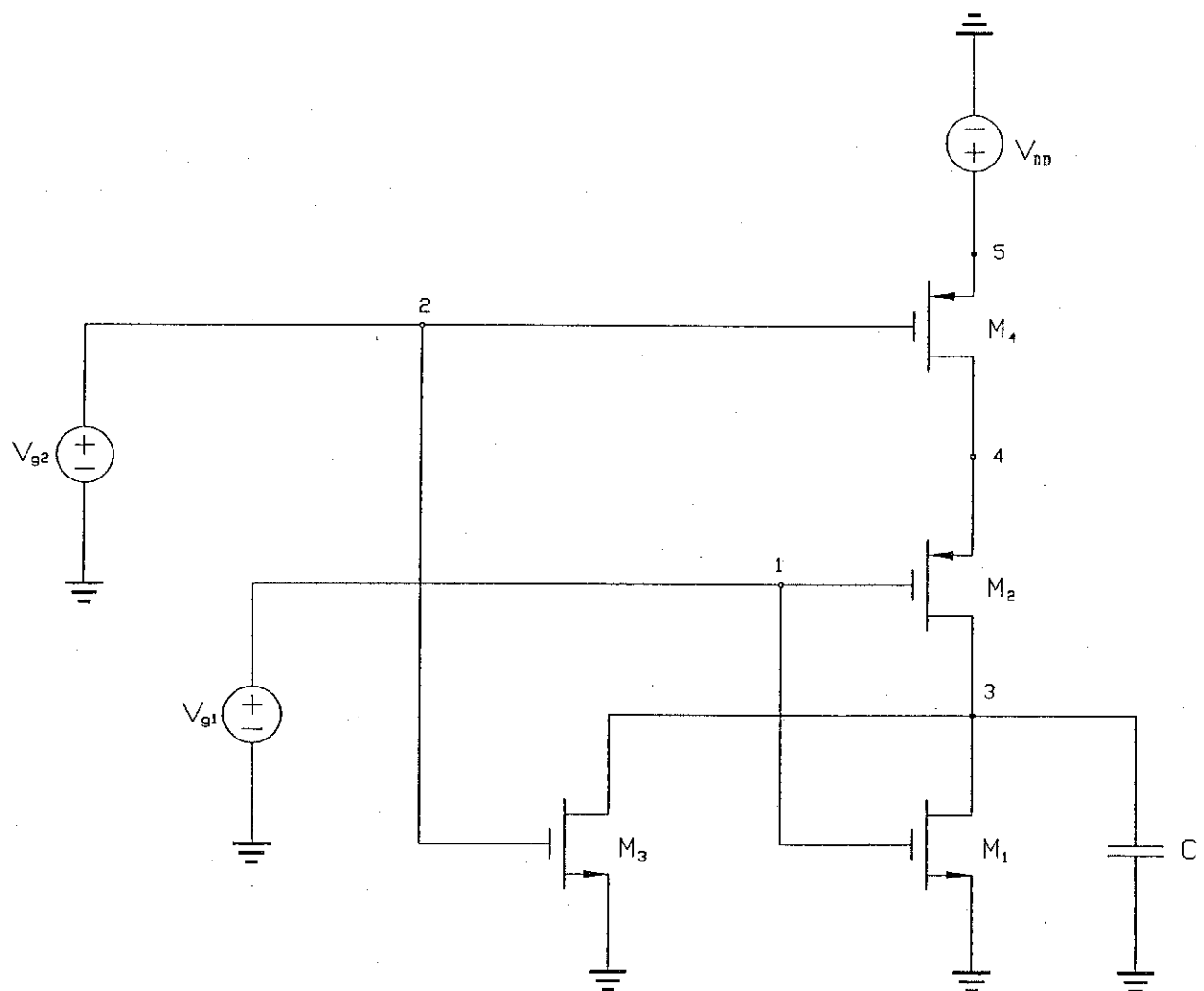


## PROJECT # 5: Transient Analysis of Digital Circuits

The circuit below represents a CMOS nor gate, with a DC supply of  $V_{DD} = 5V$  and a loading capacitor  $C = 0.25pF$ .



The device parameters are:  $K = 2 \times 10^{-5} A/V^2$ ,  $V_{Tn} = 1V$  and  $V_{Tp} = -1V$ , and all pulse sources are assumed to have:  $V_1 = 0$ ,  $V_2 = 5V$  and  $T_r = T_f = 1ns$ .

## PROBLEM 1.

Use the PMOS and NMOS transistor models to formulate the circuit equations for transient analysis. Indicate  $G$ ,  $E$ ,  $p(x)$  and  $w$  explicitly.

## PROBLEM 2.

a) Write an m - file that will perform a *partial transient analysis*, the results of which can be used to obtain a good initial approximation for the DC solution. The input arguments for this function should be matrices  $E$  and  $G$ , time  $t_{end}$ , step size  $h$  and *three*  $1 \times 7$  vectors corresponding to the different pulse sources (note that in this stage of the analysis the DC power supply is treated as a *step function*). The output should be the *waveform vectors* for all voltages, the set of *time points*, and the *number of iterations* that were needed in each time point. In other words, this function should look something like:  $[tout, out, iter] = nor(tend, h, E, G, a, b, c)$ .

b) Use this function to perform a partial transient analysis with  $t_{end} = 10\text{ns}$  and  $h = 2 \times 10^{-10}$ . Record *all* the voltage (and current) values at  $t = t_{end}$ , and use this as the initial approximation for the DC solution.

## PROBLEM 3.

a) Write an m - file that will compute a DC solution for this circuit. The input arguments for this function should be *matrix*  $G$ , the *initial guess*  $x_0$  (obtained in Problem 2), and the *convergence criterion*  $e$ . The output should contain the *solution vector* and the *number of iterations* needed for convergence. The corresponding format should be:  $[x, iter] = newt(G, e, x_0)$ .

b) Use this function to compute the *exact* DC solution (choosing  $e = 10^{-9}$  as the convergence criterion for Newton's method).

## PROBLEM 4.

a) Write an m - file that will perform a *complete transient analysis* of this circuit. The input arguments for this function should be matrices  $E$  and  $G$ , time  $t_{end}$ , step size  $h$ , DC solution  $x_0$  and *two*  $1 \times 7$  vectors that correspond to the input pulse sources (recall that in this stage the DC power supply voltage is treated as a *constant*). The output should be the *waveform vectors* for all voltages, the set of *time points*, and the *number of iterations* that were needed in each time point. Your function should have the form:  $[tout, out, iter] = nordc(tend, h, E, G, a, b, x_0)$ .

b) Use this function to obtain waveforms for voltages  $V_3(t)$  and  $V_4(t)$  in case input 1 is a LOGIC ONE and input 2 is a LOGIC ZERO (assume that  $t_{end} = 1.5 \times 10^{-7}$  sec,  $h = 2 \times 10^{-10}$ , and that the input pulse width is 100ns). Plot *both* waveforms in Matlab.

c) Perform a transient analysis of this circuit in SPICE, assuming the same input conditions as in part b). Print out your input file, and obtain plots for voltages  $V_3(t)$  and  $V_4(t)$ .

d) Compare the results of your program to those obtained using SPICE. Do you see any significant differences?